

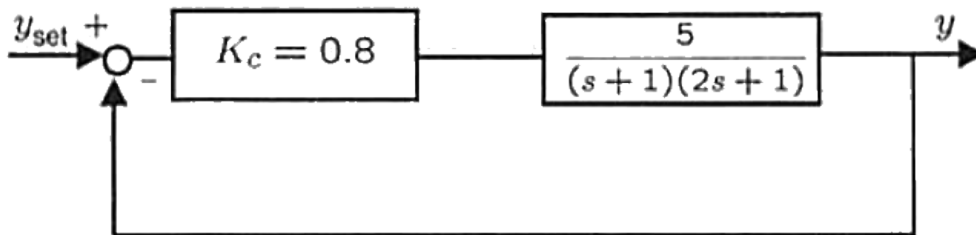
This tutorial provides some practice for the next midterm, and makes sure you understand some concepts from this week's classes.

**Question 1**

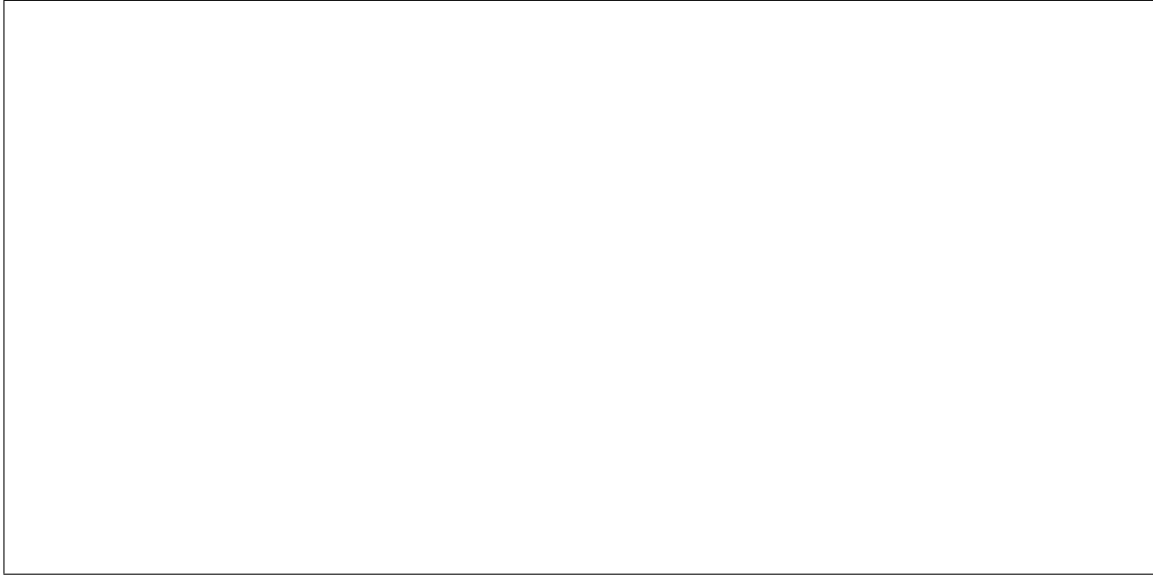
*From a previous midterm*

1. For the process transfer function  $G_p(s) = \frac{5}{(s+1)(2s+1)}$ : is it overdamped, underdamped, or critically damped? \_\_\_\_\_
2. For the same process transfer function: what are the roots?

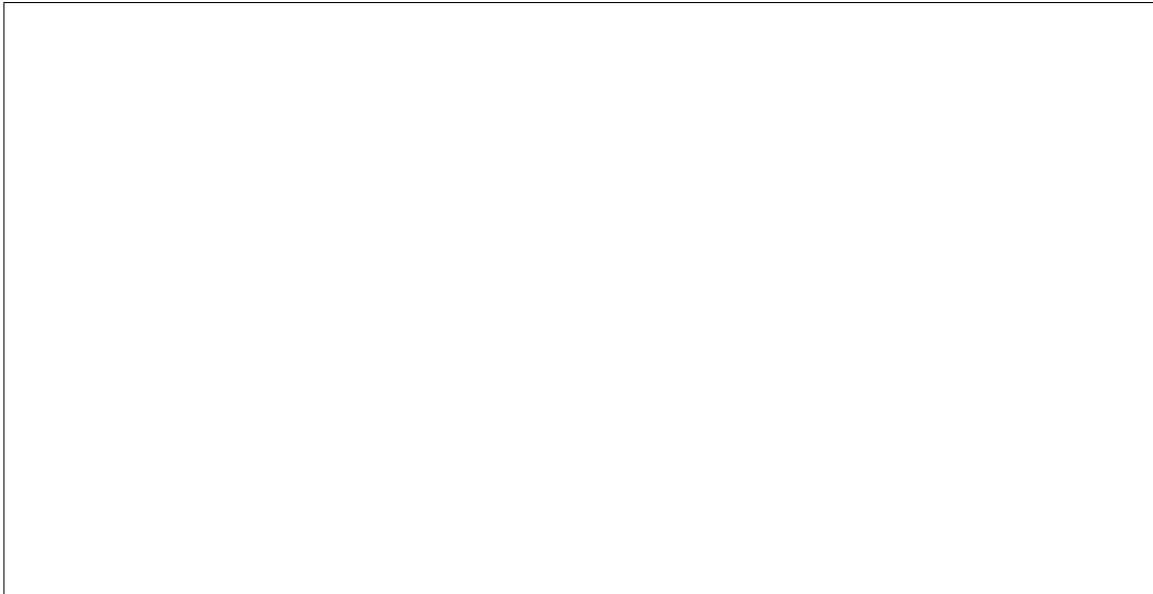
3. Write out an analytical transfer function for the closed loop response,  $\frac{y(s)}{y_{set}(s)}$ .



4. Determine the amount of offset at steady-state for a step input of 2 units in the set point. (You must do the calculations by hand, not with Simulink).



5. Describe what the time-domain characteristics of the *closed-loop* response will be: overdamped, critically damped, underdamped? And what will be the roots of the closed loop transfer function,  $\frac{y(s)}{y_{set}(s)}$ ?



## Question 2

*Challenge for extra credit* [double your tutorial grade for today]. Derive the closed-loop transfer function, from the set point to the controlled variable,  $\frac{CV(s)}{SP(s)}$  for the process  $G_p(s) = \frac{K_p}{s}$  (this is a model of a tank's height when varying the input flow - *prove it to yourself*).

Let the controller be  $G_c(s) = K_c$ , a proportional-only controller. We learned in class that P-only control has offset (never reaches the set point). However, prove mathematically that for this process there is **no offset** when making a step change in the set point,  $SP(s) = \frac{M}{s}$ . Can you explain why? Show your calculations on a separate page and hand it in by the end of the tutorial today.